# Symmetry groups in quantum relativistic dynamics. <u>https://vixra.org/abs/2306.0144</u>

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## Chapters

- 1. Introduction.
- 2. General ideas.
- 3. Symmetries in classical and quantum relativistic dynamics.

## 1. Introduction

The transformations of relativistic dynamics in the Special Theory of Relativity and quantum relativistic dynamics (it's fashionable to say Quantum Theory of Relativity) are presented in "Unified Theory 2" in one mathematical truth. We are talking about dynamic space-matter, a special case of a zero or fixed angle of parallelism, there is the Euclidean axiomatics of space-time. The Special Theory of Relativity cannot describe space-time in quantum fields with their uncertainty principle. It is impossible to fix both the time and the coordinate at the same time. And there is no quantum relativistic dynamics in the gauge fields that follow from the Dirac equation. Relativistic dynamics is represented by the Lorentz group, and the Dirac equation invariance condition  $(A_{\mu}(X) = \bar{A}_{\mu}(X) + i \frac{\partial a(X)}{\partial x_{\mu}})$  is represented by the condition  $(\frac{\partial a(X)}{\partial x_{\mu}} \equiv f'(x) = 0)$ . But this is a constant extremal of a dynamic function  $a(X) = f(x) \neq const$ . In the Yang-Mills theory , the derivative of the scalar function is added to the potential, which does not change the potential itself, in the symmetry group:

 $A_{\mu} = \Omega(x)A_{\mu}(\Omega)^{-1}(x) + i\Omega(x)\partial_{\mu}(\Omega)^{-1}(x), \text{ where } \Omega(x) = e^{i\omega},$ 

and  $\omega$ - an element of any group A and (SU (N), SO (N), Sp (N), E<sub>6</sub>, E<sub>7</sub>, E<sub>8</sub>, F<sub>4</sub>, G<sub>2</sub>), and  $A_{\mu} \rightarrow A_{\mu} + \partial_{\mu}\omega$ . In this case U(1)- describes the electromagnetic interaction, SU(2)- Weak Interactions and SU(3)- describes Strong Interactions, and so on. We will consider the conditions:  $a(X) = f(x) \neq const$ , and substantiation of symmetries in quantum relativistic dynamics (in the Quantum Theory of Relativity). 2. General representations.

Let's start the mathematical representation of symmetries with the simplest geometric figures. Regular figures on a plane retain their symmetry during rotations, inversions. For example:

**2.1. the rectangle is symmetrical** when rotated by 180<sup>°</sup>, and when rotated by 0<sup>°</sup> does not change.

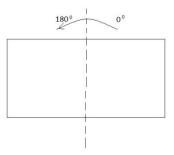


Figure 2.1.

We have two operations. Rotate 0 ° as  $R_0 = I$ , and rotate 180 ° as  $R_{180}$ . They can be multiplied by first  $R_0 * R_{180}$  turning by 0 °, then by 180 °, or vice versa:  $R_{180} * R_0$ , in the Cayley table.

C2	Ι	<i>R</i> <sub>180</sub>
Ι	Ι	R <sub>180</sub>
<i>R</i> <sub>180</sub>	R <sub>180</sub>	I

 $R_0 * R_0 = R_0 = I$ ,  $R_0 * R_{180} = \overline{R_{180}}$ .  $R_{180} * R_0 = R_{180}$ .  $R_{180} * R_{180} = R_{360} = R_0 = I$ The operation  $R_0 = I$ , does not change anything, is called the identity element of the given group. The group is defined by properties.

1). A group operation is defined, here is a turn.

2). The presence of a single element,  $R_0 = I$ ,

3). closedness, when an operation in a group gives an element that does not leave the group,

4). the presence of an inverse element  $I^{-1} = I$ , or  $R_{180}^{-1} = R_{180}$ . This is the element that undoes the previous operation of each group element.

5).associativity property: A( BC)=(AB)C. This group is called C2.

**2.2.** an example of an equilateral triangle, with rotations of 0<sup>°</sup>, 120<sup>°</sup>, and 240<sup>°</sup>.

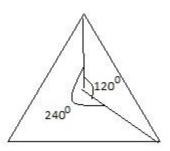


Figure 2.2

The multiplication table of a given group of rotations is compiled in exactly the same way.

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C3	Ι	<i>R</i> <sub>120</sub>	R <sub>240</sub>
Ι	Ι	<i>R</i> <sub>120</sub>	<i>R</i> <sub>240</sub>
<i>R</i> <sub>120</sub>	<i>R</i> <sub>120</sub>	R <sub>240</sub>	Ι
<i>R</i> <sub>240</sub>	R <sub>240</sub>	Ι	<i>R</i> <sub>120</sub>

All possible elements of a group, when multiplied, give the elements of the same group. The group is closed. For each element there is an inverse element and also in the group.  $R_{120}^{-1} = R_{240}$ ,  $R_{240}^{-1} = R_{120}$ .

Not only turns of figures give a group. The numbers (+1) and (-1) also form group .

3

	1	-1
1	1	-1
-1	-1	1

The group operation is multiplication. The identity element is 1. Inverse element:  $-1^{-1} = -1$ . All conditions for the group are met. This group is identical to the C 2 group. They are called isomorphic. There are also other isomorphic groups. For example, during the operation of reflection  $\sigma$  of the considered rectangle.

S2_	Ι	σ
Ι	Ι	σ
σ	σ	Ι

If we reflect the rectangle twice around the axis, we get the original object, a group with all the properties. Such a group is called S 2 and is isomorphic to the group C 2. Multiplying the coordinates of the vector (2,1) by (-1), leads to the reflection of the coordinates relative to the origin. Therefore, the group of numbers (1) and (-1) is also isomorphic.

2.3 Abelian and non-Abelian groups and subgroups. The considered groups of rotations C3 and reflections S

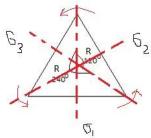


Figure 2.3.

Such rotations and reflections also do not change the triangle, and form a group. Let's write a table for it.

D3	Ι	<i>R</i> <sub>120</sub>	<i>R</i> <sub>240</sub>	$\sigma_1$	$\sigma_2$	$\sigma_3$
Ι	Ι	<i>R</i> <sub>120</sub>	<i>R</i> <sub>240</sub>	$\sigma_1$	$\sigma_2$	$\sigma_3$
<i>R</i> <sub>120</sub>	<i>R</i> <sub>120</sub>	R <sub>240</sub>	Ι	$\sigma_2$	$\sigma_3$	$\sigma_1$
R <sub>240</sub>	R <sub>240</sub>	Ι	<i>R</i> <sub>120</sub>	$\sigma_3$	$\sigma_1$	$\sigma_2$
$\sigma_1$	$\sigma_1$	$\sigma_3$	$\sigma_2$	Ι	R <sub>240</sub>	<i>R</i> <sub>120</sub>
$\sigma_2$	$\sigma_2$	$\sigma_1$	$\sigma_3$	<i>R</i> <sub>120</sub>	Ι	R <sub>240</sub>
$\sigma_3$	$\sigma_3$	$\sigma_2$	$\sigma_1$	$R_{240}$	$R_{120}$	Ι

Group C3 has subgroups D 3. Turn on  $R_{120}$  with reflection  $\sigma_1$  equals reflection  $\sigma_2$ . But if we first reflect  $\sigma_2$  and then rotate  $R_{120}$ , we get a reflection  $\sigma_3$ . That is:  $R_{120} * \sigma_1 \neq \sigma_1 * R_{120}$ . But the law of commutativity is not a property of

the group, and it does not have to be observed. The group D 3 is not abelian, the subgroup C3 is abelian. But if we choose the specified triangle, its symmetry under reflections is already broken.

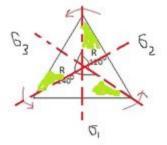


Figure 2.4

Such symmetry breaking is called spontaneous.

2.4 Representation of groups. As stated, the group operation can be any action, multiplication, rotation, inversion, whatever. Group elements can also be any abstract objects that can be replaced in isomorphic groups by prime numbers (1) and (-1) if the group is commutative. But there are also mathematical objects for which the commutativity of multiplication is not observed, for example, matrices . In other words, matrices can also be abstract elements of groups. In the considered D 3 matrix, the elements of the group can be represented by matrices, in the form:

$$I = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}, \qquad R_{120} = \frac{1}{2} \begin{pmatrix} -1 & -\sqrt{3} \\ \sqrt{3} & -1 \end{pmatrix}, R_{240} = \frac{1}{2} \begin{pmatrix} -1 & \sqrt{3} \\ -\sqrt{3} & -1 \end{pmatrix}, \\ \sigma_1 = \frac{1}{2} \begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}, \sigma_2 = \frac{1}{2} \begin{pmatrix} 1 & \sqrt{3} \\ \sqrt{3} & -1 \end{pmatrix}, \sigma_3 = \frac{1}{2} \begin{pmatrix} 1 & -\sqrt{3} \\ -\sqrt{3} & -1 \end{pmatrix}.$$

Now the operation of the group D 3 is matrix multiplication. In this case, the structure of the group is preserved:

$$R_{120} * R_{120} = R_{240}, \text{ or } \frac{1}{2} \begin{pmatrix} -1 & -\sqrt{3} \\ \sqrt{3} & -1 \end{pmatrix} * \frac{1}{2} \begin{pmatrix} -1 & -\sqrt{3} \\ \sqrt{3} & -1 \end{pmatrix} = \frac{1}{2} \begin{pmatrix} -1 & \sqrt{3} \\ -\sqrt{3} & -1 \end{pmatrix}, \text{ or }$$

$$R_{120} * \sigma_1 = \sigma_3, \text{ as: } \frac{1}{2} \begin{pmatrix} -1 & -\sqrt{3} \\ \sqrt{3} & -1 \end{pmatrix} * \frac{1}{2} \begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix} = \frac{1}{2} \begin{pmatrix} 1 & -\sqrt{3} \\ -\sqrt{3} & -1 \end{pmatrix}$$

$$\sigma_1 * R_{120} = \sigma_2, \text{ in the form: } \frac{1}{2} \begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix} * \frac{1}{2} \begin{pmatrix} -1 & -\sqrt{3} \\ 0 & 1 \end{pmatrix} = \frac{1}{2} \begin{pmatrix} 1 & \sqrt{3} \\ \sqrt{3} & -1 \end{pmatrix}$$

Rotation matrices do not commute with reflection matrices along the specified axes. But the rotation matrices commute with each other. The product  $R_{120} * R_{240} = I$ , or  $\frac{1}{2} \begin{pmatrix} -1 & -\sqrt{3} \\ \sqrt{3} & -1 \end{pmatrix} * \frac{1}{2} \begin{pmatrix} -1 & \sqrt{3} \\ -\sqrt{3} & -1 \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} = I$ , gives The single element of the group. All matrices are invertible.  $R_{120}^{-1} = R_{240}, \frac{1}{2} \begin{pmatrix} -1 & -\sqrt{3} \\ \sqrt{3} & -1 \end{pmatrix}^{-1} = \frac{1}{2} \begin{pmatrix} -1 & \sqrt{3} \\ -\sqrt{3} & -1 \end{pmatrix}$ . The inverse element of the matrix group is represented by the inverse matrix:  $\sigma_1^{-1} = \sigma_1$ , or  $\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}^{-1} = \begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$ .

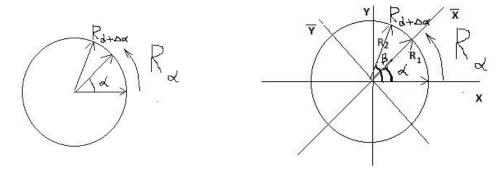
The analysis of the abstract operations of a group can thus be replaced by the study of the properties of matrices. But matrices can also be considered as operators acting on vectors. For example, when rotating a vector

$$\begin{pmatrix} 0 \\ 1 \end{pmatrix} \text{by} R_{120} , \qquad \text{we get:} \frac{1}{2} \begin{pmatrix} -1 & -\sqrt{3} \\ \sqrt{3} & -1 \end{pmatrix} * \begin{pmatrix} 0 \\ 1 \end{pmatrix} = \begin{pmatrix} -\sqrt{3}/2 \\ -1/2 \end{pmatrix} \text{ rotated vector, or:} \begin{pmatrix} 0 \\ 1 \end{pmatrix} \text{on } R_{240}, \qquad \text{we get} \frac{1}{2} \begin{pmatrix} -1 & \sqrt{3} \\ -\sqrt{3} & -1 \end{pmatrix} * \begin{pmatrix} 0 \\ 1 \end{pmatrix} = \begin{pmatrix} \sqrt{3}/2 \\ -1/2 \end{pmatrix}.$$

#### Figure 2.5

Multiplying the remaining matrices by any of these three vectors will translate the vector into one of these three. We get the same symmetrical triangle. That is, matrices are representations of operations.

2.5. In group theory there are many theorems: discrete groups, normal subgroups, classes, factor - groups .... Let us consider the groups A and, in physical theories. In the previous group, for example D 3, we considered the symmetries of a triangle under rotations and reflections. Similarly, one can consider the symmetries of a square in the group D4 for 4 turns, in a regular pentagon D 5 for 5 turns, a hexagon D 6 for 6 turns ... A regular ( $N \rightarrow \infty$ ) square turns into a circle, with the radius rotated by the angle ( $\alpha$ ). The circle is invariant under rotations through any angle ( $\alpha$ ). But here there are no elements of the groups considered earlier (*R*) and ( $\sigma$ ).



#### Figure 2.6

In such a symmetry group of a circle, a group parameter is introduced, by the angle of rotation  $R_{\alpha}$ . In this group, we obtain a continuous transition from one element of the group  $(R_{\alpha})$  to another  $(R_{\alpha+\Delta\alpha})$ . These are the groups L and. Here there is  $(R_0 = I)$  an identity element, the inverse element of the group  $(R_{\alpha}^{-1} = R_{2\pi-\alpha})$ . The elements of the group are also represented by matrices. If we consider rotations of the coordinate system  $XY \rightarrow \overline{X}\overline{Y}$ , we obtain for  $R_1(R_{X1}R_{Y1})$  and  $R_2(R_{X2}R_{Y2})$ :  $R_1 * R_2 = |R_1||R_2|\cos(\beta - \alpha) = (R_{X1}R_{X2} + R_{Y1}R_{Y2})$ ,

$$\begin{split} |R_1||R_2|\cos(\beta - \alpha) &= |R_1|\cos(\alpha)|R_2|\cos(\beta) + |R_1|\sin(\alpha)|R_2|\sin(\beta),\\ \cos(\beta - \alpha) &= \cos(\alpha)\cos(\beta) + \sin(\alpha)\sin(\beta),\\ \cos(\beta + \alpha) &= \cos(\beta - (-\alpha)) = \cos(-\alpha)\cos(\beta) + \sin(-\alpha)\sin(\beta),\\ \cos(\beta + \alpha) &= \cos(\alpha)\cos(\beta) - \sin(\alpha)\sin(\beta)\\ |R_1|* (|R_2|\cos(\beta + \alpha) = \bar{X}) = |R_1|\cos(\alpha)* (|R_2|\cos(\beta) = X) - |R_1|\sin(\alpha)* (|R_2|\sin(\beta) = Y)\\ \bar{X} &= X\cos(\alpha) - Y\sin(\alpha). \\ |R_1||R_2|\sin(\beta + \alpha) &= |R_1||R_2|\cos(90 - (\beta + \alpha)) = |R_1||R_2|\cos((90 - \alpha) - \beta)\\ |R_1||R_2|\sin(\beta + \alpha) &= |R_1||R_2|\cos(90 - \alpha)\cos(\beta) + |R_1||R_2|\sin(90 - \alpha)\sin(\beta)\\ |R_1|* (|R_2|\sin(\beta + \alpha) = \bar{Y}) = |R_1|\sin(\alpha)* (|R_2|\cos(\beta) = X) + |R_1|\cos(\alpha)* (|R_2|\sin(\beta = Y)) \end{split}$$

$$Y = X\sin(\alpha) + Y\cos(\alpha).$$

Finally, we get the transformations:

$$\begin{vmatrix} X = X\cos(\alpha) - Y\sin(\alpha) \\ \overline{Y} = X\sin(\alpha) + Y\cos(\alpha) \end{vmatrix} \text{ or } \begin{pmatrix} \overline{X} \\ \overline{Y} \end{pmatrix} = \begin{pmatrix} X \\ Y \end{pmatrix} \begin{pmatrix} \cos(\alpha) & -\sin(\alpha) \\ \sin(\alpha) & \cos(\alpha) \end{pmatrix}$$
$$\begin{pmatrix} \overline{X} \\ \overline{Y} \end{pmatrix} = \begin{pmatrix} X \\ Y \end{pmatrix} * R_{\alpha} \quad \text{where is} \quad R_{\alpha} = \begin{pmatrix} \cos(\alpha) & -\sin(\alpha) \\ \sin(\alpha) & \cos(\alpha) \end{pmatrix} \text{ the matrix of the group A and.}$$

The previou

$$R_{120} = \begin{pmatrix} \cos(120) & -\sin(120) \\ \sin(120) & \cos(120) \end{pmatrix} = \frac{1}{2} \begin{pmatrix} -1 & -\sqrt{3} \\ \sqrt{3} & -1 \end{pmatrix}$$

This is a (  $R_{\alpha}$ ) SO (2) matrix , i.e. a Special ( det (  $R_{\alpha}$ )=1) Orthogonal (  $R_{\alpha}(R_{\alpha})^{T} = I$ ) matrix where the transposed

matrix  $(R_{\alpha})^{T} = (R_{\alpha})^{-1}$  is equal to the inverse. This is  $(R_{\alpha})$  the rotation matrix, abelian. The matrix of the scaling operation  $\begin{pmatrix} M & 0 \\ 0 & M \end{pmatrix}$  with the parameter (M=2), performs  $\begin{pmatrix} 2 & 0 \\ 0 & 2 \end{pmatrix} \begin{pmatrix} 1 \\ 1 \end{pmatrix} = \begin{pmatrix} 2 \\ 2 \end{pmatrix}$  an increase (M > 1) or decrease (0 < M < 1) of the original vector. The parameter (M) can be taken out of brackets, then we

will get  $M\begin{pmatrix} 1 & 0\\ 0 & 1 \end{pmatrix}$  a group generator in brackets, not attached to the elements of the group. Angle ( $\alpha$ ) the group parameter  $R_{\alpha} = \begin{pmatrix} \cos(\alpha) & -\sin(\alpha)\\ \sin(\alpha) & \cos(\alpha) \end{pmatrix}$  is also taken out  $R_0 = I$ , the rotation by 0<sup>°</sup> does nothing, it gives the identity matrix. Turning an angle  $(\Delta \alpha \rightarrow 0)$  gives  $(R_{\Delta \alpha} = I + \Delta \alpha L)$  transformation where (L)rotation generator. Then  $(R_{\alpha+\Delta\alpha} = R_{\Delta\alpha}R_{\alpha})$  to rotate by an angle ( $\alpha + \Delta \alpha$ ), you must first rotate by an angle ( $\alpha$ ), then by an angle ( $\Delta \alpha$ ). Substituting the values, we get:  $(R_{\alpha + \Delta \alpha} = (I + \Delta \alpha L)R_{\alpha} = R_{\alpha} + \Delta \alpha LR_{\alpha})$ . Further, in the usual order, we obtain:  $(R_{\alpha + \Delta \alpha} - R_{\alpha} = \Delta \alpha LR_{\alpha})$ ,  $lim \frac{R_{\alpha + \Delta \alpha} - R_{\alpha}}{\Delta \alpha \to 0} = LR_{\alpha}$ ,  $\frac{dR_{\alpha}}{d\alpha} = LR_{\alpha}$ ,  $\frac{dR_{\alpha}}{R_{\alpha}} = Ld\alpha$ ,  $R_{\alpha} = e^{\alpha L}$ , solution of the differential equation, with the group generator  $(\frac{dR_{\alpha}}{d\alpha})_0 = L$ . These equations are similar to the Schrödinger equation:  $\frac{dU}{dt} = -iHU$ , with solutions:  $U = e^{-itH}$ . Here the group generator is represented by the Hamilton operator, and instead of turning by an angle, time is considered. In our case of rotations, the group generator is equal to the derivative of the group elements at zero rotation angle. We take the derivatives, substitute the value of the angle and get the group generator.

$$\frac{dR_{\alpha}}{d\alpha} = \begin{pmatrix} -\sin(0) & -\cos(0) \\ \cos(0) & -\sin(0) \end{pmatrix} = \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} = L. \text{ Or } \frac{dR_{\alpha}}{d\alpha} = LR_{\alpha}, \text{ in the form: } \frac{dR_{\alpha}}{d\alpha} = \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} \cos(\alpha) & -\sin(\alpha) \\ \sin(\alpha) & \cos(\alpha) \end{pmatrix}.$$

Here:  $\cos^2(\alpha) + \sin^2(\alpha) = 1$ , as expected. Then the rotated and original vector is represented as:  $\bar{V} = e^{\alpha (1 - 0)V}$ ,

where:  $e^{\alpha \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}}$  is the matrix of the group element. Now we rotate the vector by an angle ( $\alpha$ ) without using trigonometric functions. The generators themselves say a lot about the band itself. For example, the scale generator  $e^{m \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}} = e^{\begin{pmatrix} m & 0 \\ 0 & m \end{pmatrix}}$  is represented as a group element. The scale factor is:  $M = e^m$  the exponent of the group parameter (m).

**2.6.** The elements of the groups L and are found by matrix exponentiation of the generators of the Lie groups. The elements themselves are considered as generators acting on the vector. These operators change the vector. But the invariant always remains unchanged in the group. Group generator L and:  $L = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$  changes the element of the Lie group  $R_{\alpha} = e^{\pm \alpha \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}}$ , as the scaling operator. Acting  $R_{\alpha}$  on the column of point coordinates, we obtain radially diverging (converging) points with a constant angle ( $\alpha$ ). The group generator  $L = \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$  gives the group element  $R_{\alpha} = e^{\pm \alpha \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}}$ , as a point moving in a circle. The length of the vector is constant. D. The group generator  $L = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$  gives the group element  $R_{\alpha} = e^{\pm \alpha \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}}$  gives the group element  $R_{\alpha} = e^{\pm \alpha \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}}$ , the Lorentz group. This takes place:  $ch^2(\alpha) - sh^2(\alpha) = 1$ , as expected. Recall the graphs of these functions  $Y = Y_0 ch \left(\alpha = \frac{X=Z}{Y_0}\right)$  in the form:

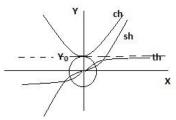


Figure 2.7

Here the Lorentz group  $\Lambda = \begin{pmatrix} ch(\alpha) & sh(\alpha) \\ sh(\alpha) & ch(\alpha) \end{pmatrix}$ , together with  $ch^2(\alpha) - sh^2(\alpha) = 1$  and elements of the group in the form  $R_{\alpha} = e^{\pm \alpha \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}}$  represented in hyperbolic functions  $e^z = ch(z) + sh(z)$ . At the same time, we derived transformations of the relativistic dynamics  $R_{\alpha} = \begin{pmatrix} cos(\alpha) & -sin(\alpha) \\ sin(\alpha) & cos(\alpha) \end{pmatrix}$  of the Lie group matrix, with the generator already in the trigonometric  $e^{iz} = cos(z) + isin(z)$  functions  $R_{\alpha} = e^{i\alpha \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}}$  of the group elements. There is a problem in the relativistic solutions of the invariant Dirac equation. The action of a quantum cannot  $\hbar = \Delta p \Delta \lambda = F \Delta t \Delta \lambda$  be fixed in space  $\Delta \lambda$  or time  $\Delta t$ . This is due to the non-zero  $(\varphi \neq const)$  angle of parallelism (X-) or (Y-) trajectory  $(X\pm)$  or  $(Y\pm)$  space-matter quantum. There is only a certain probability of action. Transformations of the relativistic dynamics of the wave  $\Psi$  - function of the quantum field with the probability density ( $|\Psi|^2$ ) of interaction in (X+) the field (Fig. 3) correspond to the Globally Invariant  $\Psi(X) = e^{-i\alpha}\overline{\Psi}(X)$ , a = const Lorentz group. These transformations correspond to rotations in the plane of the circle S, and relativistically - to the invariant Dirac equation.

$$i\gamma_{\mu}\frac{\partial\psi(X)}{\partial x_{\mu}} - m\psi(X) = 0$$
, and  $\left[i\gamma_{\mu}\frac{\partial\overline{\psi}(X)}{\partial x_{\mu}} - m\overline{\psi}(X)\right] = 0$ 

Such invariance gives the conservation laws in the equations of motion. For transformations of relativistic dynamics in hyperbolic motion,

$$\psi(X) = e^{a(X)}\overline{\psi}(X). \qquad ch(aX) = \frac{1}{2}(e^{aX} + e^{-aX}) \cong e^{aX}. \qquad a(X) \neq const.$$
$$\left[i\gamma_{\mu} \frac{\partial\overline{\psi}(X)}{\partial x_{\mu}} - m\overline{\psi}(X)\right] + i\gamma_{\mu} \frac{\partial a(X)}{\partial x_{\mu}}\overline{\psi}(X) = 0$$

The invariance of conservation laws is violated. To save them, calibration fields are introduced. They compensate for the extra term in the equation.

$$A_{\mu}(X) = \overline{A}_{\mu}(X) + i\frac{\partial a(X)}{\partial x_{\mu}}, \text{ and } i\gamma_{\mu} \left[\frac{\partial}{\partial x_{\mu}} + iA_{\mu}(X)\right] \psi(X) - m\psi(X) = 0$$

Now, substituting the value  $\Psi(X) = e^{a(X)}\overline{\Psi}(X)$  of  $a(X) \neq const$  the wave function into such an equation, we obtain an invariant equation of relativistic dynamics.

$$i\gamma_{\mu}\frac{\partial\psi}{\partial x_{\mu}} - \gamma_{\mu}A_{\mu}(X)\psi - m\psi = i\gamma_{\mu}\frac{\partial\overline{\psi}}{\partial x_{\mu}} + i\gamma_{\mu}\frac{\partial a(X)}{\partial x_{\mu}}\overline{\psi} - \gamma_{\mu}\overline{A}_{\mu}(X)\overline{\psi} - i\gamma_{\mu}\frac{\partial a(X)}{\partial x_{\mu}}\overline{\psi} - m\overline{\psi} = 0$$

$$i\gamma_{\mu}\frac{\partial\overline{\psi}}{\partial x_{\mu}} - \gamma_{\mu}\overline{A}_{\mu}(X)\overline{\psi} - m\overline{\psi} = 0$$

$$i\gamma_{\mu}\left[\frac{\partial}{\partial x_{\mu}} + i\overline{A}_{\mu}(X)\right]\overline{\psi} - m\overline{\psi} = 0$$

$$i\gamma_{\mu}\left[\frac{\partial}{\partial x_{\mu}} + i\overline{A}_{\mu}(X)\right]\overline{\psi} - m\overline{\psi} = 0$$

This equation is invariant to the original equation

$$i\gamma_{\mu} \left[ \frac{\partial}{\partial x_{\mu}} + iA_{\mu}(X) \right] \psi(X) - m\psi(X) = 0$$
$$A_{\mu}(X) = \overline{A}_{\mu}(X), \text{ and } \qquad A_{\mu}(X) = \overline{A}_{\mu}(X) + i\frac{\partial a}{\partial x}$$

in conditions

the presence of a scalar boson  $(\sqrt{(+a)(-a)} = ia(\Delta X) \neq 0) = const$ , within the gauge  $(\Delta X) \neq 0$  field (Fig. 3). These conditions  $(\frac{\partial a(X)}{\partial x_{\mu}} \equiv f'(x) = 0)$  give constant extremals  $(f_{max})$  dynamic  $a(X) = f(x) \neq const$  space-matter in global invariance. And there are no scalar bosons here. These are:  $A_{\mu}(X) = \bar{A}_{\mu}(X) + i\frac{\partial a(X)}{\partial x_{\mu}}$ , known gauge transformations. a(X)- 4-vector  $(A_0, A_1, A_2, A_3)$  electromagnetic scalar  $(\varphi = A_0)$  and vector  $(\vec{A} = A_1, A_2, A_3)$  potential in Maxwell electrodynamics:  $\vec{E} = -\nabla \varphi - \frac{\partial \vec{A}}{\partial t}$ , and  $\vec{B} = -\nabla x \vec{A}$ , gradient and curl, or  $F_{\mu\nu} = \partial_{\mu}A_{\nu} - \partial_{\nu}A_{\mu}$ , with tensor  $(F_{\mu\nu})$ ,  $(E_X, E_Y, E_Z, E_X, E_Y, E_Z)$  components and Lorentz transformations. The derivative of the scalar function is added to such a potential, which does not change the potential itself. This is the key point. In the Yang-Mills theory, it is represented by a symmetry group,  $A_{\mu} = \Omega(x)A_{\mu}(\Omega)^{-1}(x) + i\Omega(x)\partial_{\mu}(\Omega)^{-1}(x)$ , where  $\Omega(x) = e^{i\omega}$ , and  $\omega$ is an element of any (SU (N), SO (N), Sp (N), E\_6, E\_7, E\_8, F\_4, G\_2) of the group L and,  $A_{\mu} \rightarrow A_{\mu} + \partial_{\mu}\omega$ . In reality, this is a fixed state of a dynamic function:  $K_Y = \psi + Y_0$ , in quantum relativistic dynamics. Relatively speaking, at each fixed point: a  $(\frac{X \equiv Z}{Y_0}) = const$ , there is its own (angle of inclination of the branches) hyperbolic cosine,  $K_Y = Y_0 ch(\frac{X \equiv Z}{Y_0}) \equiv e^{a(\frac{X \equiv Z}{Y_0})}$ , already in the orthogonal  $(YZ \perp X)$ ) plane, and, moreover, outside the dynamic in quantum relativistic dynamics  $(Y_0)$ . Thus, scalar bosons in gauge fields are created artificially to eliminate the shortcomings of the Theory of Relativity in quantum fields.

## 3. symmetries in classical and quantum relativistic dynamics

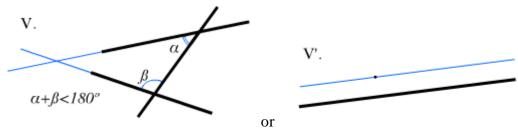
**3.1. Lorentz transformations** in physics are considered as:  $\bar{x} = \frac{x+wt}{\sqrt{1-w^2}}$ ,  $\bar{t} = \frac{t+wx}{\sqrt{1-w^2}}$ , c = 1. These two formulas are represented as a single matrix expression.

$$\frac{1}{\sqrt{1-w^2}} \begin{pmatrix} 1 & w \\ w & 1 \end{pmatrix} \begin{pmatrix} t \\ x \end{pmatrix} = \frac{1}{\sqrt{1-w^2}} \begin{pmatrix} t+wx \\ wt+x \end{pmatrix} = \begin{pmatrix} \bar{t} \\ \bar{x} \end{pmatrix}. \qquad \Lambda = \begin{pmatrix} \operatorname{ch}(\alpha) & \operatorname{sh}(\alpha) \\ \operatorname{sh}(\alpha) & \operatorname{ch}(\alpha) \end{pmatrix}$$

The matrix action converts non-primed vector coordinates to primed ones. The angle of rotation in hyperbolic transformations is related to the hyperbolic arc tangent  $\alpha = arc \ th(w)$  and find this angle from the speed, which approaches unity:  $w \rightarrow (c = 1)$ . The mathematical apparatus of group theory is thus quite universal **in the Euclidean axiomatics** of space-time. They are known:

"A point is that, part of which is nothing") ("Beginnings" of Euclid). and whether the Point is that which has no parts,
 Line - length without width.

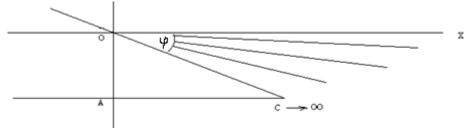
3. And the 5th postulate about parallel straight lines that do not intersect. If a line intersecting two lines forms interior one-sided angles less than two lines, then, extended indefinitely, these two lines will meet on the side where the angles are less than two lines.

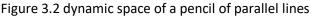


drawing. 3.1 Euclidean axiomatics

That is, through a point outside the line, you can draw only one straight line, parallel to the line.

**3.2.** in fact, in the "Unified Theory 2", undecidable in the Euclidean axiomatic are noted contradictions. That is, many lines in one line (length without width), again a line. Is it a line or many lines? Similarly, the set of points in one point is again a point. Is it a point or a set of them? The Euclidean Elements do not provide answers to such questions. well-known problems 5th postulate, the solution of which opened Lobachevski geometry and Riemannian space.





There are real facts of the dynamic space of a bunch of straight lines that do not intersect, that is, parallel to the original line AC at infinity, presented in the "Unified Theory 2". And moving along the line (AC), there will be a dynamic space nearby, which we will not be able to get into in principle.

Infinity cannot be stopped, so this already dynamic space always exists. And already the properties of this dynamic  $(\varphi \neq const)$  spaces are presented as properties of matter, the main property of which is movement. There is no matter outside such space, and there is no space without matter. Space-matter is one and the same.

In such a dynamic space-matter, the Euclidean axiomatic is presented as a special case zero ( $\varphi = 0$ ) angle of parallelism. At the same time solving the set problem exactly straight lines in one straight parallel lines as " length without breadth ".

The main property of a dynamic space-matter is a dynamic ( $\varphi \neq const$ ) angle of parallelism. In this case, the Euclidean space in the XYZ axes loses its meaning.

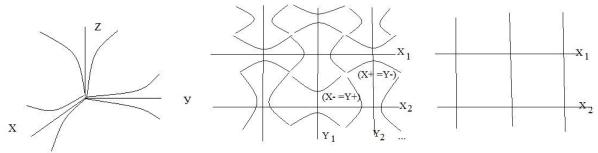
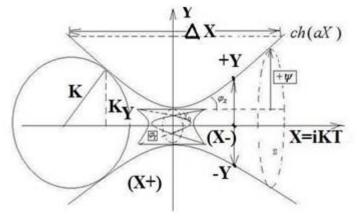


figure 3.3 dynamic space-matter

In "Unified Theory 2 " (), Transformations of relativistic dynamics in the Special Theory of Relativity and quantum relativistic dynamics (it is fashionable to say Quantum Relativity Theory), are presented in one mathematical truth, form. We are talking about the relativistic dynamics of the radius-vector of a dynamic sphere with a non-stationary Euclidean space-time, on the trajectory (X-) or (Y-) of the quantum ( $X \pm$ ) ( $Y \pm$ ), respectively, of the dynamic space-matter. Consider, for example, a quantum ( $X \pm$ ) of a dynamic space-matter.



#### Figure 3.4 quantum of dynamic space-matter

We see that the dynamic radius-vector (K) in the sphere with non-stationary Euclidean space-time has projections (K <sub>Y</sub>) in the plane of the circle of the dynamic sphere, and projections (K <sub>X</sub>) on the (X-) trajectories. On (n) convergence, as we already know and see, there are two trajectories of (Y ±) quantum closed on (Y -). As already noted, at each point fixed in the experiment with ( $i\psi = \sqrt{(+\psi)(-\psi)}$ ) wave function, there is a hyperbolic cosine with different slope angles of the graph branches. In the section of the circle, the point fixed in the experiment with ( $i\psi = \sqrt{(+\psi)(-\psi)}$ ) wave functions, with different radii of the circle in different fixed points (X-) of the trajectory of the space-matter quantum. As we see at fixed points, fixed experimental facts, both representations of the Lorentz group are valid and correspond to the truth. Terms of  $A_{\mu}(X) = \bar{A}_{\mu}(X) + i \frac{\partial a(X)}{\partial x_{\mu}}$ 

the Dirac equation and conditions  $A_{\mu} = \Omega(x)A_{\mu}(\Omega)^{-1}(x) + i\Omega(x)\partial_{\mu}(\Omega)^{-1}(x)$ , where:  $\Omega(x) = e^{i\omega}$ , in the Yang-Mills theory are not violated. Here:

 $e^{i\omega} = \cos \omega + i \sin \omega$ ), and  $(i \sin \omega \equiv K_Y = \sqrt{(+ \sin \omega)(- \sin \omega)} = i\psi = \sqrt{(+\psi)(-\psi)}$ . The identity matrices of  $(R_\alpha)$  group elements,  $\cos^2(\alpha) + \sin^2(\alpha) = 1$  for any rotations and  $(\Lambda)$  groups:  $ch^2(\alpha) - sh^2(\alpha) = 1$ , and their derivatives in the form of group generators (reducible to zero initial conditions) are unchanged. But the very dynamics of such conditions, that is, the quantum relativistic dynamics of the dynamic sphere radius vector with non-stationary Euclidean space-time, we have lost it  $a(X) \neq const$ . represented by a matrix with a dynamic wave function:  $i\psi = i\sin \omega \equiv \pm K_Y$  in an experiment, as an argument, as a fixed fact of reality. But there is no theory, or models, equations of such "hidden processes", as we see. It must be said that in the dynamic space-matter, there is a space-matter, which we cannot get into in principle. We can't get in, by definition.

Let us present a tabular (comparative) analysis of the representations of the Lorentz groups of the relativistic dynamics of the Special Theory of Relativity and quantum relativistic dynamics, in full, without the condition (c=1) of the speed of light.

$$R_{\alpha} = \begin{pmatrix} \cos(\alpha) & -\sin(\alpha) \\ \sin(\alpha) & \cos(\alpha) \end{pmatrix}, \cos^{2}(\alpha) + \sin^{2}(\alpha) = 1$$

$$R_{\alpha} = \begin{pmatrix} \cos(\alpha) & -\sin(\alpha) \\ \sin(\alpha) & \cos(\alpha) \end{pmatrix}, \cos^{2}(\alpha) + \sin^{2}(\alpha) = 1$$

$$R_{\alpha} = \begin{pmatrix} ch\left(\frac{x \equiv z}{y_{0}}\right) & sh\left(\frac{x \equiv z}{y_{0}}\right) \\ sh\left(\frac{x \equiv z}{y_{0}}\right) & ch\left(\frac{x \equiv z}{y_{0}}\right) \\ sh\left(\frac{x \equiv z}{y_{0}}\right) & ch\left(\frac{$$

 $R_{\alpha} * \Lambda_{(x/y_0)} = e^{\alpha * \begin{pmatrix} 1 & 0 \end{pmatrix}} * e^{(x/y_0) * \begin{pmatrix} 1 & 0 \end{pmatrix}}$ , simultaneous dynamics of circular and hyperbolic motion Radius vector (its vertices) of dynamic $(y_0 \neq const)$  spheres.

Special theory of relativity	Lorentz group
$\bar{x} = \frac{x - wt}{\sqrt{1 - (w/c)^2}}, \bar{t} = \frac{t - wx/c^2}{\sqrt{1 - (w/c)^2}}$	$\Lambda = \frac{1}{\sqrt{1 - (w/c)^2}} \begin{pmatrix} 1 & w/c^2 \\ w & 1 \end{pmatrix}, \Lambda * \begin{pmatrix} t \\ \chi \end{pmatrix} = \begin{pmatrix} \overline{t} \\ \overline{\chi} \end{pmatrix}$
$\overline{w} = \frac{x - wt}{t - wx/c^2},$	$\frac{1}{\sqrt{1-(w/c)^2}} \begin{pmatrix} 1 & w/c^2 \\ w & 1 \end{pmatrix} \begin{pmatrix} t \\ x \end{pmatrix} = \frac{1}{\sqrt{1-(w/c)^2}} \begin{pmatrix} t - wx/c^2 \\ -wt + x \end{pmatrix} = \begin{pmatrix} \bar{t} \\ \bar{x} \end{pmatrix},$
	$\bar{t} = \frac{t - wx/c^2}{\sqrt{1 - (w/c)^2}}$ . $\bar{x} = \frac{-wt + x}{\sqrt{1 - (w/c)^2}}$ . exactly the same dynamics
quantum relativistic dynamics	(Quantum Theory of Relativity)
$\overline{K_Y} = \frac{a_{11}K_Y - cT}{\sqrt{1 - (a_{22})^2}}, \overline{T} = \frac{a_{22}T - K_Y/c}{\sqrt{1 - (a_{22})^2}}.$	$Q = \frac{1}{\sqrt{1 - (a_{22})^2}} \binom{a_{22}}{c} \frac{1/c}{c} Q * \binom{T}{K_Y} = \binom{\bar{T}}{\bar{K}}$
$a_{11} = \cos(\varphi_Y) \neq const,$	$\frac{1}{\sqrt{1-(a_{22})^2}} \begin{pmatrix} a_{22} & 1/c \\ c & a_{11} \end{pmatrix} \begin{pmatrix} K_Y \end{pmatrix} = \frac{1}{\sqrt{1-(a_{22})^2}} \begin{pmatrix} a_{22}T - K_Y/c \\ a_{11}K_Y - cT \end{pmatrix} = \begin{pmatrix} \overline{T} \\ \overline{K} \end{pmatrix}$
$a_{22} = \cos(\varphi_X) \neq const,$ $\overline{W} = \frac{a_{11}K_Y - cT}{a_{22}T - K_Y/c} = \frac{a_{11}W_Y - c}{a_{22} - W_Y/c'}$	$(a_{11} \neq a_{22}) \neq const,$
$a_{22}T - K_Y/c  a_{22} - W_Y/c'$	$ \begin{pmatrix} a_{22} & 1/c \\ c & a_{11} \end{pmatrix} = a_{11} * a_{22} - c * \frac{1}{c} = 0. a_{11} * a_{22} = c * \frac{1}{c} = 1 . $
	from where follows: $a_{11} * a_{22} = \cos(\varphi_Y) * \cos(\varphi_X) = 1$ ,

In the case of quantum relativistic dynamics, as we see, the symmetry condition follows: under the conditions  $(a_{11} \neq a_{22}) \neq const$ , we get:  $a_{11} * a_{22} = cos(\uparrow \varphi_Y) * cos(\downarrow \varphi_X) = 1$ , in nonzero values angles of parallelism  $(\varphi_Y \neq 0)$ ,  $(\varphi_X \neq 0)$ , for the conditions of the denominator  $\sqrt{1 - (a_{22})^2} \neq 0$ ,  $(X \pm)$  quantum. Exactly the same transformations  $(Y \pm)$  quantum, with the terms of the denominator  $\sqrt{1 - (a_{11})^2} \neq 0$ . But the angles of parallelism cannot be 90°. This means  $(\varphi \neq 90^\circ)$  that there are limit angles of parallelism, which correspond to the constants of interactions, in the form:  $cos(\varphi_Y)_{max} = \alpha(Y \pm) = 1/137.036$ , and:  $cos^2(\varphi_X)_{max} = G(X \pm) = 6.67 * 10^{-8}$ . As you can see, the quantum oscillations themselves (the answer to the question WHY) are determined by the limiting angles of parallelism, in quantum relativistic dynamics. In numerical terms,  $(T = (K_Y/c) \approx (3 * 10^{-14} sm)/3 * 10^{10} \approx 10^{-24})s$ , period fluctuations and the frequency  $(\nu = \frac{1}{T})^2 = \rho$ , in the unified Criteria of Evolution, are connected with the limiting densities (as a cause) of quantum fields of space-matter.

In the "Unified Theory 2 ", we considered the unified Criteria for the Evolution of dynamic space-matter in multidimensional space-time. In particular, charge:  $q = \Pi K (Y + = X -)$  in electro (Y + = X -) magnetic fields, and mass:  $m = \Pi K (X + = Y -)$  in gravity (X+=Y-) mass fields . We have also considered models of proton quantum fields:

 $(X \pm = p^+) = (Y - = \gamma_0^+)(X + = \nu_e^-)(Y - = \gamma_0^+), \text{ and: } (Y \pm = e^-) = (X + = \nu_e^-)(Y - = \gamma^+)(X + = \nu_e^-) \text{ electron.}$ Then the conditions:  $a_{22}^2 * a_{11} = \cos^2(\varphi_X) \cos(\varphi_Y) = 1$ , quantum relativistic dynamics  $(X \pm)$  quantum take the form:  $(X \pm) = (X + = Y -)^2 * (Y + = X -), \text{ or: } \Pi K * \cos^2(\varphi_X) \cos(\varphi_Y) = 1 * \Pi K.$ 

$$(\Pi K(X+=Y-) = m_0 = 1) * cos^2(\varphi_X)_{max} cos(\varphi_Y)_{max} = 1 * (\Pi K(Y+=X-) = q_0 = 1).$$

Scale  $(a_{22})$ , in quantum state: $a_{22}^2 * a_{11} = \cos^2(\varphi_X) \cos(\varphi_Y) = 1 \text{ matrix} \begin{pmatrix} 1 & \alpha \\ 1 & 1 \end{pmatrix}^2 = (1 - \alpha)^2$ . Then:

$$(m_0 = 1) * (1 - \alpha)^2 (\cos^2(\varphi_X)_{max} = G) (\cos(\varphi_Y)_{max} = \alpha) = 1 * q,$$

 $q(Y + = X -) = (1 - \alpha)^2 * G * \alpha = (1 - 1/137.036)^2 * 6.67 * 10^8 * (1/137.036) = 4.8 * 10^{-10}$ . We have obtained an electric charge in the symmetry group of its quantum relativistic dynamics, in known relations:  $\alpha = q^2/\hbar c$ ,  $w = \alpha c$ ,  $\alpha = \cos(\varphi_Y)_{max} = a_{11}$ ,  $\cos(\varphi_Y) = \cos(\varphi_X)$ , already as symmetries  $(X \pm = Y \mp)$  fields of a single (X + = Y -), (X - = Y +) dynamic space-matter.

In the same way, by scaling the symmetry group  $Q = e^{(X,Y)*L}$  of quantum relativistic dynamics (it is fashionable to say in the Quantum Relativity Theory), but already of mass fields, one can search for the mass spectrum of elementary particles. This is different from the symmetries of Lorentz groups in gauge fields.

#### Super symmetries in quantum relativistic dynamics.

Chapters

- 4. Introduction.
- 5. Representation of symmetry groups in quantum relativistic dynamics.
- 6. Super symmetries in quantum relativistic dynamics.

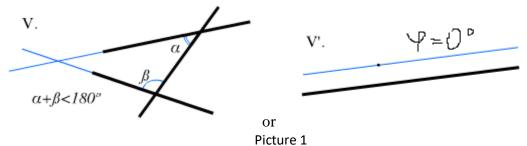
#### 1. Introduction

Super symmetries in quantum relativistic dynamics are considered in the same mathematical models as symmetries. Symmetries in quantum relativistic dynamics (it's fashionable to say Quantum Relativity Theory) were considered in the same mathematical truth with Lorentz group symmetries in gauge fields. There is a difference in the representation of symmetry groups in the relativistic dynamics of the Special Theory of Relativity, as Lorentz groups and symmetry groups in quantum relativistic dynamics (Quantum Theory of Relativity). In the first case, the symmetry of the Lorentz group was considered in space-time with the Euclidean axiomatics. These are the well-known axioms of Euclid.

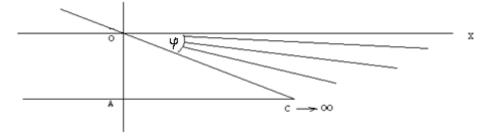
1. "A point is that, part of which is nothing") ("Beginnings" of Euclid). or a point is that which has no parts,

#### 2. Line - length without width.

3. And the 5th postulate about parallel straight lines that do not intersect. If a line intersecting two lines forms interior one-sided angles less than two lines, then, extended indefinitely, these two lines will meet on the side where the angles are less than two lines.

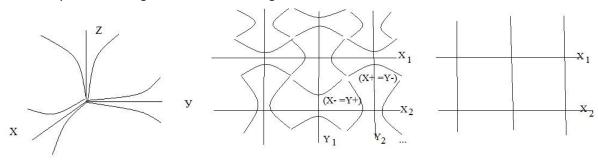


In this case, the angle of parallelism ( $\varphi = 0$ ) is zero, and the set of straight lines in one "... length without width " is also a straight line. This is the problem of the Euclidean axiomatics. It does not exist in the dynamic space-matter:



#### Figure 2

with non-zero ( $\phi \neq 0$ )  $\neq const$ , and dynamic angle of parallelism. Infinity (AC  $\rightarrow \infty$ )cannot be stopped, so dynamic space-matter always exists. In a grid of Euclidean straight lines





we do not see a dynamic space-matter, and the Euclidean space itself loses its meaning. Rather, we are talking about non-stationary Euclidean space within the dynamic angle of parallelism. Such a dynamic space-matter has its own axioms as facts that do not require proof. In the case of fixing the angle of parallelism, which is especially important in fixed experimental data, we get the Euclidean axiomatics of space-time, or variants of the Riemannian space (including Lobachevsky geometry), in modern theories , with the uncertainty principle, the wave function and the technology of quantum theories. And it is in such a dynamic space-matter that we have already considered the symmetries of quantum relativistic dynamics.

2. Representation of symmetry groups in quantum relativistic dynamics.

In the symmetry of quantum relativistic dynamics, we have obtained transformations of quantum relativistic dynamics (Quantum Theory of Relativity), by analogy with the classical relativistic dynamics of Einstein's Special Theory of Relativity represented by the Lorentz group. Let's present their tabular (comparative) analysis in the form: Table 1

Special theory of relativity( $c = 1$ )	Lorentz group
$\bar{x} = \frac{x - wt}{\sqrt{1 - (w)^2}},$ $\bar{x} = \frac{t - wx}{t - wx}$	$\Lambda = \frac{1}{\sqrt{1 - (w)^2}} \begin{pmatrix} 1 & w \\ w & 1 \end{pmatrix}, \Lambda * \begin{pmatrix} t \\ \chi \end{pmatrix} = \begin{pmatrix} \bar{t} \\ \bar{\chi} \end{pmatrix}$
$t = \frac{1}{\sqrt{1 - (w)^2}}$ $\overline{w} = \frac{x - wt}{w}.$	$\frac{1}{\sqrt{1-(w)^2}} \begin{pmatrix} 1 & w \\ w & 1 \end{pmatrix} \begin{pmatrix} t \\ x \end{pmatrix} = \frac{1}{\sqrt{1-(w)^2}} \begin{pmatrix} t - wx \\ -wt + x \end{pmatrix} = \begin{pmatrix} \overline{t} \\ \overline{x} \end{pmatrix},$
t - wx'	$\bar{t} = \frac{t - wx}{\sqrt{1 - (w)^2}}$ . $\bar{x} = \frac{-wt + x}{\sqrt{1 - (w)^2}}$ . exactly the same dynamics

quantum relativistic dynamics( $c \neq 1$ )	(Quantum Theory of Relativity)
$\overline{K_Y} = \frac{a_{11}K_Y - cT_X}{\sqrt{1 - (a_{22})^2}}, \ \overline{T_X} = \frac{a_{22}T_X - K_Y/c}{\sqrt{1 - (a_{22})^2}}.$	$Q = \frac{1}{\sqrt{1 - (a_{22})^2}} \begin{pmatrix} a_{22} & 1/c \\ c & a_{11} \end{pmatrix}, Q * \begin{pmatrix} T \\ K_Y \end{pmatrix} = \begin{pmatrix} \overline{T} \\ \overline{K} \end{pmatrix}$
$a_{11} = \cos(\varphi_{\rm Y}) \neq const,$	$\frac{1}{\sqrt{1-(a_{22})^2}} \binom{a_{22}}{c} \frac{1/c}{a_{11}} \binom{T}{K_Y} = \frac{1}{\sqrt{1-(a_{22})^2}} \binom{a_{22}T - K_Y/c}{a_{11}K_Y - cT} = \binom{\bar{T}}{\bar{K}}$
$a_{22} = \cos(\varphi_X) \neq const,$ $\overline{W} = \frac{a_{11}K_Y - cT_X}{a_{11}W_Y - c} = \frac{a_{11}W_Y - c}{a_{11}W_Y - c}.$	$(a_{11} \neq a_{22}) \neq const,$
$W = \frac{1}{a_{22}T_X - K_Y/c} = \frac{1}{a_{22} - W_Y/c'}$	$\binom{a_{22}}{c}  \frac{1/c}{a_{11}} = a_{11} * a_{22} - c * \frac{1}{c} = 0. a_{11} * a_{22} = c * \frac{1}{c} = 1.$
	from where follows: $a_{ref} * a_{ref} = \cos(a_r) * \cos(a_r) = 1$

A remarkable point in the symmetry of quantum relativistic dynamics is the condition  $(a_{22} = 1)$  Euclidean axiomatics, in which:  $\cos(\varphi_X = 0) = (a_{22}) = 1$ , in the denominator  $Q = \frac{1}{\sqrt{1-(a_{22})^2}} \begin{pmatrix} a_{22} & 1/c \\ c & a_{11} \end{pmatrix}$  we get zero. Therefore, keeping **the mathematical truth**, we consider the space of the quantum itself under the conditions (c=1), and obtain the following relations:

$$Q = \frac{1}{\sqrt{1 - (a_{22})^2}} \begin{pmatrix} a_{22} & 1\\ 1 & a_{11} \end{pmatrix} = \frac{0}{0} = 0, \quad \text{or} \quad \begin{pmatrix} a_{22} & 1\\ 1 & a_{11} \end{pmatrix} = 0.$$
$$a_{22} * a_{11} - 1 = 0. \quad a_{22} * a_{11} = 1.$$

This is a very interesting condition:  $[(\cos(\varphi_Y = 0) = 1) * (\cos(\varphi_X = 0) = 1) = 1] - [1 * 1] = 0$ , it is valid in the Euclidean axiomatics. The determinant of such a matrix is zero if two columns or two rows are equal. Formally, in Euclidean space, in this representation:

$$[(\cos(\varphi_Y = 0) = 1) * (\cos(\varphi_X = 0) = 1), \text{ these conditions are:} \qquad a_{22} * a_{11} = 1$$

are respected. But the same conditions are observed in the non-stationary Euclidean space, with the same mathematical truth:  $a_{22} * a_{11} = 1$ , but in the form:  $\cos(\varphi_Y \neq 0) * \cos(\varphi_X \neq 0) = 1$ . Here, in the Euclidean space, we do not see the dynamics inside the space-matter quantum, but this does not mean that there is no such dynamics inside the quantum. This is quantum relativistic dynamics, which is not in the Euclidean axiomatics ( $\varphi = 0$ ) of space-time. And these are the conditions of quantum relativistic dynamics.

The second moment in the symmetry of a single (X+=Y-), (X-=Y+) space-matter in models

proton: 
$$(X \pm = p^+) = (Y - = \gamma_0^+)(X + = \nu_e^-)(Y - = \gamma_0^+),$$
 or  $(X \pm = p^+) = (Y \pm)^2(X \pm)$ :  
d electron:  $(Y \pm = e^-) = (X - = \nu_e^-)(Y + = \gamma^+)(X - = \nu_e^-),$  or  $(Y \pm = e^-) = (X \pm)^2(Y \pm)$ 

and electron:  $(Y \pm = e^-) = (X - = v_e^-)(Y + = \gamma^+)(X - = v_e^-)$ , or  $(Y \pm = e^-) = (X \pm)^2(Y \pm)$ in dynamic space-matter ("Unified Theory 2"). The conditions for such a symmetry are represented as:  $a_{22}^2 * a_{11} = \cos^2(\varphi_X) \cos(\varphi_Y) = 1$ , quantum relativistic dynamics  $(a_{11} \neq a_{22}) \neq const$  for  $(X \pm)$  a quantum.

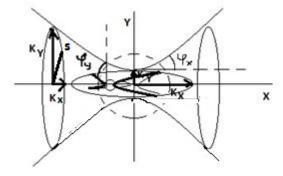


Figure 4

Thus, we have a group generator  $\begin{pmatrix} (a_{22})^2 & 1/c \\ c & a_{11} \end{pmatrix} = 0$ , or:  $a_{22}^2 * a_{11} = \cos^2(\varphi_X) \cos(\varphi_Y) = 1$ . In this case,  $\cos^2(\varphi_X) = \sqrt{1 - \sin^2(\varphi_X)}$ ,  $\sin(\varphi_X) = \frac{w_Y}{c}$ ,  $w_Y = \frac{K_Y}{T_Y}$ , and  $\cos^2(\varphi_X) = \sqrt{1 - (\frac{w_Y}{c})^2}$ , we obtain the same relativistic correction as in the Lorentz group, but for quantum relativistic dynamics  $\cos(\varphi_X)$ 

correction as in the Lorentz group, but for quantum relativistic dynamics  $\cos(\varphi_Y)$ .

 $\begin{array}{ll} (X \pm) = (X + = Y -)^2 * (Y + = X -), & \text{or:} & \Pi K * \cos^2(\varphi_X) \cos(\varphi_Y) = 1 * \Pi K. \\ (\Pi K (X + = Y -) = m_0 = 1) * \cos^2(\varphi_X)_{max} \cos(\varphi_Y)_{max} = 1 * (\Pi K (Y + = X -) = q_0 = 1), \end{array}$ 

in the uniform Criteria for the Evolution of charge (Y + = X -), and mass(X + = Y -) fields of the proton and electron.

This is the key point when the symmetry is: $\cos^2(\varphi_X)\cos(\varphi_Y) = 1$  scaled,

$$\Pi K * \cos^2(\varphi_X) \cos(\varphi_Y) = 1 * \Pi K$$

charge and mass fields of a single( $X \pm$ ) = ( $Y \mp$ ) space-matter, in this case. In this case, the limiting angles of parallelism of quantum fields correspond to the interaction constants in local basis vectors in the already Riemannian space:

$$a_{11} = 1 * 1 * \cos(\varphi_Y)_{max} = \cos(\varphi_Y)_{max} = \alpha = \frac{1}{137.036'},$$
  
$$a_{22} = 1 * 1 * \cos(\varphi_X)_{max} = \cos(\varphi_X)_{max} = \sqrt{G} = 6.67 * 10^{-8}, \text{ or } a_{22}^2 = \cos^2(\varphi_X) = G.$$

The transformations of already quantum relativistic dynamics ( $\varphi_X \neq const$ ), and ( $\varphi_Y \neq const$ ), are scaled by a matrix, with the limiting parameters of a quantum of space-matter (Figure 4) in such dynamics in the form:

$$\begin{pmatrix} \cos(\varphi_X = 0) = 1 & \cos(\varphi_Y)_{max} = \alpha \\ ch\left(\frac{X=0}{Y_0}\right) = 1 & ch\left(\frac{Y=0}{X_0}\right) = 1 \end{pmatrix}^2 = \begin{pmatrix} 1 & \alpha \\ 1 & 1 \end{pmatrix}^2 = (1-\alpha)^2, \text{ and}$$

We get:,  $(1 - \alpha)^2 * G * \alpha (\Pi K = m_0 = 1) = 1 * (\Pi K = q = 1)$ or ultimately an electric charge,  $q(Y = X) = (1 - \alpha)^2 * G * \alpha = (1 - 1/137.036)^2 * 6.67 * 10^8 * (1/137.036) = 4.8 * 10^{-10}$ ,

in its quantum relativistic dynamics. The charge in this representation corresponds to the relations:

$$\alpha = \frac{q^2}{\hbar c} = \frac{1}{137.036}$$

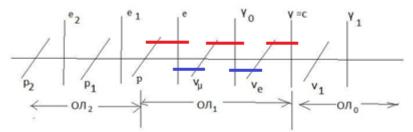
In strict mathematical truths. What is remarkable about quantum relativistic dynamics is that the isotropy of the space-time of the Euclidean sphere is exactly the same as the isotropy along each axis of the dynamic ellipsoid:  $(K_Y \downarrow)^2 + (K_X = cT_X \uparrow)^2 = (s)^2$  the non-stationary Euclidean space-time. The dynamics of the period ( $T_X$ ) corresponds to the deceleration or acceleration of time along the axis (X). In this case of quantum relativistic dynamics, we are talking about the dynamics of the space-time itself of the space-matter quantum, under the conditions of the group generator (Q = 0), when events do not exit the dynamic ellipsoid. The space of an ellipsoid is a hidden space (Fig. 3), which we cannot get into from the Euclidean space-time. It is correct to say that it does not exist in Euclidean space.

$$(+K_Y)(-K_Y) + (K_X = cT_X \uparrow)^2 = (s = 0)^2$$
, or:  $(cT_X)^2 = (K_Y)^2$ , or:  $cT_X = K_Y$ .

And this means that the surface of a dynamic ellipsoid, the light reaches simultaneously along each axis. Or, any point of a photon has the speed of light. We are talking, at the same time, about the Euclidean isotropy of the non-stationary Euclidean space in quantum relativistic dynamics. There is no such space in the axes (XYZ) of the stationary Euclidean space. But the opposite would be better. In real space-matter, with Euclidean isotropy in non-zero angles of parallelism with non-stationary Euclidean space, there is no stationary Euclidean space with zero angle of parallelism in (XYZ) axes. This is the reason not for the locality of simultaneous events, as already the facts of experiments.

### 3. Supersymmetries in quantum relativistic dynamics.

In the quantum coordinate system of dynamic space-matter, we talked about the first  $(0\Lambda_1)$  level, the Area of Localization of indivisible quanta of space-matter  $(p)(e)(\nu_{\mu})(\gamma_0)(\nu_e)(\gamma)$ , ("Unified Theory 2").



#### Figure 5

In this Area of Localization of indivisible  $(O\Pi_1)$  level quanta, there are  $(Y + = e^-) = (X - = p^+)$ charge  $(Y + = \gamma_0^-) = (X - = \nu_{\mu}^+)$ ,  $(Y + = \gamma^+) = (X - = \nu_e^-)$ , and mass:  $(Y - = e^-) = (X + = \nu_{\mu}^+)$  isopotentials  $(Y - = \gamma_0^-) = (X + = \nu_e^+)$ , substances in this case, in their structuring. There is a spectrum of masses of these indivisible quanta of space-matter. m(p) = 938,28MeV,  $G = 6,67 * 10^{-8}$ .  $m_e = 0,511 MeV$ ,  $(m_{\nu_{\mu}} = 0,27 MeV)$ ,

$$\begin{pmatrix} \frac{X=K_X}{K} \end{pmatrix}^2 (X-) = \cos^2 \varphi_X = \left(\sqrt{G}\right)^2 = G, \qquad \left(\frac{Y=K_Y}{K}\right)(Y-) = \cos \varphi_Y = \alpha = \frac{1}{137,036}$$

$$m = \frac{F=\Pi^2}{Y''} = \left[\frac{\Pi^2 T^2}{Y} = \frac{\Pi}{(Y/K^2)}\right] = \frac{\Pi Y = m_Y}{\left(\frac{Y^2}{K^2} = \frac{G}{2}\right)}, \text{ from where:} \qquad 2m_Y = Gm_X \text{ , or:}$$

$$(\Pi K = m_Y) = \Pi K * (\cos^2(\varphi_X) = G) * (\cos(\varphi_Y) = 1) * (\Pi K = m_X), \text{ in quantum relativistic dynamics}$$

$$m = \frac{F=\Pi^2}{X''} = \left[\frac{\Pi^2 T^2}{X} = \frac{\Pi}{(X/K^2)}\right] = \frac{\Pi X = m_X}{\left(\frac{X^2}{K^2} = \frac{\alpha^2}{2}\right)}, \text{ whence} \qquad 2m_X = \alpha^2 m_Y, \text{ or:}$$

 $2(\Pi K = m_X) = \Pi K * (\cos^2(\varphi_Y) = \alpha^2) * (\cos(\varphi_X) = 1) * (\Pi K = m_Y)$ , in quantum relativistic dynamics From such quantum relativistic dynamics, calculations of the spectrum in the quantum coordinate system follow.

2

$$m_X = \alpha^2 \ m_Y/2 \ , \qquad \text{or:} \qquad (\alpha/\sqrt{2}) * \Pi K * (\alpha/\sqrt{2}) = \frac{\alpha^2 m(e)}{2} = \ m(\nu_e^{\pm}) = 1.36 * 10^{-5} MeV \ ,$$
$$m_Y = G m_X/2, \text{ or:} (\sqrt{G/2}) * \Pi K * (\sqrt{G/2}) = \frac{G m(p)}{2} = \ m(\gamma_0^{\pm}) = 3.13 * 10^{-5} MeV \ ,$$
similarly:
$$m(\gamma) = \frac{G m(\nu_{\mu})}{2} = 9,1 * 10^{-9} MeV.$$

In a single  $(Y \pm = X \mp)$  or (Y + = X -), (Y - = X +) space-matter of indivisible structural forms of indivisible quanta  $(Y \pm)$  and  $(X \pm)$ . The reality of such representations follows from the calculations.

 $(Y \pm = e^{-}) = (X + = v_e^{-})(Y - = \gamma^+)(X + = v_e^{-})$  electron, where: HO $\Lambda(Y \pm) = K\Im(Y + )K\Im(Y - )$ , and  $(X \pm = p^+) = (Y - = \gamma_0^+)(X + = v_e^{-})(Y - = \gamma_0^+)$  proton, where: HO $\Lambda(X \pm) = K\Im(X + )K\Im(X - )$ ,

we separate electromagnetic (Y + = X -) fields from mass fields (Y - = X +) in the form:

$$(X +)(X +) = (Y -) \text{and} \frac{(X +)(X +)}{(Y -)} = 1 = (Y +)(Y -); (Y += X -) = \frac{(X +)(X +)}{(Y -)}, \text{ or:} \frac{(X + v_e/2)(\sqrt{2*G})(X + v_e/2)}{(Y - v^+)} = q_e(Y +)$$

$$q_e = \frac{(m(v_e)/2)(\sqrt{2*G})(m(v_e)/2)}{m(\gamma)} = \frac{(1.36 * 10^{-5})^2 * \sqrt{2} * 6,67 * 10^{-8}}{4 * 9,07 * 10^{-9}} = 4,8 * 10^{-10} \text{ CFCE}$$

$$(Y +)(Y +) = (X -) \text{and} \frac{(Y +)(Y +)}{(X -)} = 1 = (X +)(X -); (Y += X -) = \frac{(Y -)(Y -)}{(X +)}, \text{ or:} \frac{(Y - v_e^+)(\alpha^2)(Y - v_e^+)}{(X + v_e^-)} = q_p(Y += X -),$$

$$q_p = \frac{(m(\gamma_0^+)/2)(\alpha^2/2)(m(\gamma_0^+)/2)}{m(v_e^-)} = \frac{(3,13 * 10^{-5}/2)^2}{2 * 137,036^2 * 1.36 * 10^{-5}} = 4,8 * 10^{-10} \text{ CFCE}$$

Such coincidences cannot be accidental. Here we fix the fact that quantum relativistic dynamics is real and its calculations give results. A control check of the reality of such facts follows already from the experimental facts. For a proton wavelength  $\lambda_p = 2,1 * 10^{-14}$  cm, its frequency  $(\nu_{\gamma_0^+}) = \frac{c}{\lambda_p} = 1,4286 * 10^{24}$   $\Gamma \mu$ is formed by the frequency

$$(\gamma_0^+)$$
 of quanta, with mass  $2(m_{\gamma_0^+})c^2 = G\hbar(\nu_{\gamma_0^+})$ 

 $1e = 5,62 * 10^{26} MeV, \text{ or}(m_{\gamma_0^+}) = \frac{\frac{G\hbar(v_{\gamma_0^+})}{2c^2}}{2c^2} = \frac{6,67*10^{-8}*1,0545*10^{-27}*1,4286*10^{24}}{2^{*9*10^{20}}} = 5,58 * 10^{-32}e = 3,13 * 10^{-5} MeV$ Similarly for an electron  $\lambda_e = 3,86 * 10^{-11} cm$ , its frequency  $(v_{v_e^-}) = \frac{c}{\lambda_e} = 7,77 * 10^{20} \Gamma q$ , is formed by the frequency  $(v_e^-)$  of quanta, with mass  $2(m_{v_e^-})c^2 = \alpha^2\hbar(v_{(v_e^-)})$ , where  $\alpha(Y - ) = \frac{1}{137,036}$  is a constant, we obtain for the neutrino mass:

$$(m_{\nu_e^-}) = \frac{\alpha^2 \hbar(\nu_{(\nu_e^-)})}{2c^2} = \frac{1*1,0545*10^{-27}*7,77*10^{20}}{(137,036^2)*2*9*10^{20}} = 2,424*10^{-32}c = 1,36*10^{-5}MeV, \text{ or:}$$

stable particles with annihilation products in a single  $(Y \mp = X \pm)$  space-matter:

$$(X \pm e) = (Y - = \gamma_o)(X + = \nu_e)(Y - = \gamma_o) = \left(\frac{2\gamma_o}{G} - \frac{\nu_e}{\alpha^2}\right) = 938,275 \text{ MeV}; \text{ proton and:}$$
$$(Y \pm e) = (X - = \nu_e)(Y + = \gamma)(X - = \nu_e) = \left(\frac{2\nu_e}{2} + \frac{\gamma * \alpha}{\alpha^2}\right) = 0,511 \text{ MeV}; \text{ electron.}$$

Such coincidences are also not accidental and they already follow from the experimental data. If in the symmetries of quantum relativistic dynamics we used the symmetry:

$$\operatorname{IK} * \cos^2(\varphi_X) \cos(\varphi_Y) = 1 * \operatorname{IK}$$

from which the quantum relativistic dynamics of the electric charges of the proton and electron follows, now we consider the same  $(\cos^2(\varphi_X) \cos(\varphi_Y) = 1)$ symmetry of quantum relativistic dynamics:

$$(\Pi K)^2 * \cos^2(\varphi_X) \cos(\varphi_Y) = 1 * (\Pi K)^2,$$

but already for a quadratic form. This symmetry follows from the calculations of the interaction constant of two charges, which we represent in the unified Evolution Criteria as:

 $\hbar c * \propto = q^2$ , or:  $((\Pi K)^2 = \hbar c) * (\cos^2(\varphi_X = 0) = 1) * (\cos(\varphi_Y)_{max} = \propto) = 1 * (\Pi K = q)^2$ . In this case, we single out the relativistic invariant ( $\hbar c = const$ ), but already in quantum relativistic dynamics

$$\cos^{2}(\varphi_{X})\cos(\varphi_{Y}) = 1 \quad \text{or:} \quad \begin{pmatrix} \cos^{2}(\varphi_{X}) & 0 \\ 0 & \cos(\varphi_{Y}) \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \quad \text{this invariant, in the form:} \\ ((\Pi K)^{2} = \hbar c) * (\cos^{2}(\varphi_{X}) = 1)(\cos(\varphi_{Y}) = \alpha) = 1 * (\Pi K = q)^{2}. \\ \frac{(\Pi K = q)^{2}}{(\cos^{2}(\varphi_{X}) = 1) * (\cos(\varphi_{Y})_{max} = \alpha)} = \hbar c, \quad \text{or:} \quad \frac{(4,8 * 10^{-10})^{2}}{(1/137.036)} = 3.157 * 10^{-17} \cong (\hbar c = 3.1647 * 10^{-17})$$

Similarly, in the same mathematical model of quantum relativistic dynamics, the following takes place:  $((\Pi K = m_c)^2) * (\cos^2(m_c) = G)(\cos(m_c = 0) = 1) = 1 * ((\Pi K)^2 = \hbar c) \quad \text{or}$ 

$$(m_1 = m_0)^2 + (m_0)^2 + (m_0)^2 = 0)(\cos(\phi_Y = 0) = 1)^2 = 1 + (m_0)^2 + m_0, \text{ of } (m_0)^2 + (m_0)^2$$

- c

$$(m_0)^2 = \frac{\pi}{G} = \frac{6.67 \times 10^{-8}}{6.67 \times 10^{-8}} \cong 1 \times 4.8 \times 10^{-10}$$
, gives charge, or: (m\_0)

Its matrix representation with the interaction constant in the form:

$$\begin{pmatrix} \sqrt{G} * m_0 & 0\\ 0 & \sqrt{G} * m_0 \end{pmatrix} = \hbar c,$$
$$(m_0 - v^{\pm}) \sqrt{G} * (m_0 - v^{\pm}) \cdot c$$

This invariant, we scale with real quanta,  $\sqrt{G} * (m_0 = \gamma_0^{\pm})\sqrt{G} * (m_{0=}\nu_e^{\pm})$ , mass isopotential, and act by the group generator:  $Q = \begin{pmatrix} (a_{22})^2 & 1 \\ 1 & a_{11} \end{pmatrix} = 0$ , from which the quantum relativistic dynamics follows:  $(a_{22})^2 a_{11} = 1$ , taking into account the classical relations :  $\pi = \frac{l}{d} = \frac{2(X-1)}{2Y_0}$ :

$$\begin{pmatrix} \operatorname{ch}\left(\frac{X=0}{Y_0}\right) = 1 & -\pi * \operatorname{ch}(1) \\ \pi * (\cos(\varphi_Y)_{max} = \propto) & \cos(\varphi = 0) = 1 \end{pmatrix} = (1 + \alpha * \operatorname{ch}(1) * \pi^2).$$

Ultimately, the relations of quantum relativistic dynamics follow:  $(a_{22})^2 a_{11} = 1$ :

$$\begin{pmatrix} \sqrt{G} * \gamma_0^{\pm} & 0\\ 0 & \sqrt{G} * \nu_e^{\pm} \end{pmatrix} * (1 + \alpha * \operatorname{ch}(1) * \pi^2) = \hbar c = (\gamma_0^{\pm}) G(\nu_e^{\pm}) * (1 + \alpha * \operatorname{ch}(1) * \pi^2) \text{, or:}$$
$$(\hbar c = 3.1647 * 10^{-17}) = (3,13 * 10^{-5}) * 6.67 * 10^{-8} * (1.36 * 10^{-5}) * (1 + \frac{1.543 * (3.14)^2}{137.036}) = 3.155 * 10^{-17}.$$

In physical terminology, we say that the specified bosons and fermions form a relativistic invariant ( $\hbar c$ ), in the specified matrix representation. Here we talked about the mass isopotential:  $(Y - = \gamma_0^-) = (X + = \nu_e^+)$ , in the quantum coordinate system. Similarly, by scaling the quantum relativistic dynamics of something else:  $(Y - = e^-) = (X + = \nu_u^+)$ the mass isopotential, we get the same result.

$$\frac{1}{2} * \begin{pmatrix} G * e/\pi & 0 \\ 0 & G * \nu_{\mu}/\pi \end{pmatrix} (1 + \alpha * \pi) = \hbar c, \text{ or: } (e)(G/\pi)^2 (\nu_{\mu}) * (1 + \alpha * \pi) = \hbar c,$$
  
(0.5) \* (0.511) \* (6.67 \* 10<sup>-8</sup>/3.14)<sup>2</sup> \* (0.27) \* (1 + 3.14/137.036) =  $\frac{3.18 * 10^{-17}}{3.18 * 10^{-17}} = (\hbar c = \frac{3.1647 * 10^{-17}}{3.1647 * 10^{-17}}).$ 

Thus, we have obtained the same relativistic invariant ( $\hbar c$ ), in the indicated matrix representation of the symmetry of bosons and fermions in quantum relativistic dynamics. Other In other words, we are talking about the supersymmetry ( $\Pi K$ )<sup>2</sup> \* cos<sup>2</sup>( $\varphi_X$ ) cos( $\varphi_Y$ ) = 1 \* ( $\Pi K$ )<sup>2</sup> of these bosons and fermions, in the quantum relativistic dynamics of the isopotentials of the quantum coordinate system.